

Dr. Chun's Numb3rs & Løgic

Game of Craps



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Game of Craps



A player rolls **two dice**, and the sum of the two numbers that appear is observed.



If the sum on the first roll is **7** or **11**, the player **wins** the game immediately. If the sum on the first roll is **2**, **3**, or **12**, the player **loses** the game immediately.

If the sum on the first roll is **4**, **5**, **6**, **8**, **9**, or **10**, then the two dice are rolled again and again until the sum is either **7** or the **original value**.

If the **original value** is obtained a second time before 7 is obtained, then the player **wins**.

If the sum **7** is obtained before the original value is obtained a second time, then the player **loses**.



Compute the **probability** that the player will **win**.



- **Random Variables**

X = First number

Y = Second number

- **Sample Space, $S = (X, Y)$** 36 possible outcomes!

1, 1	1, 2	1, 3	1, 4	1, 5	1, 6
2, 1	2, 2	2, 3	2, 4	2, 5	2, 6
3, 1	3, 2	3, 3	3, 4	3, 5	3, 6
4, 1	4, 2	4, 3	4, 4	4, 5	4, 6
5, 1	5, 2	5, 3	5, 4	5, 5	5, 6
6, 1	6, 2	6, 3	6, 4	6, 5	6, 6

- **Probability Distribution of $Z = X + Y$ (Sum of the two numbers)**

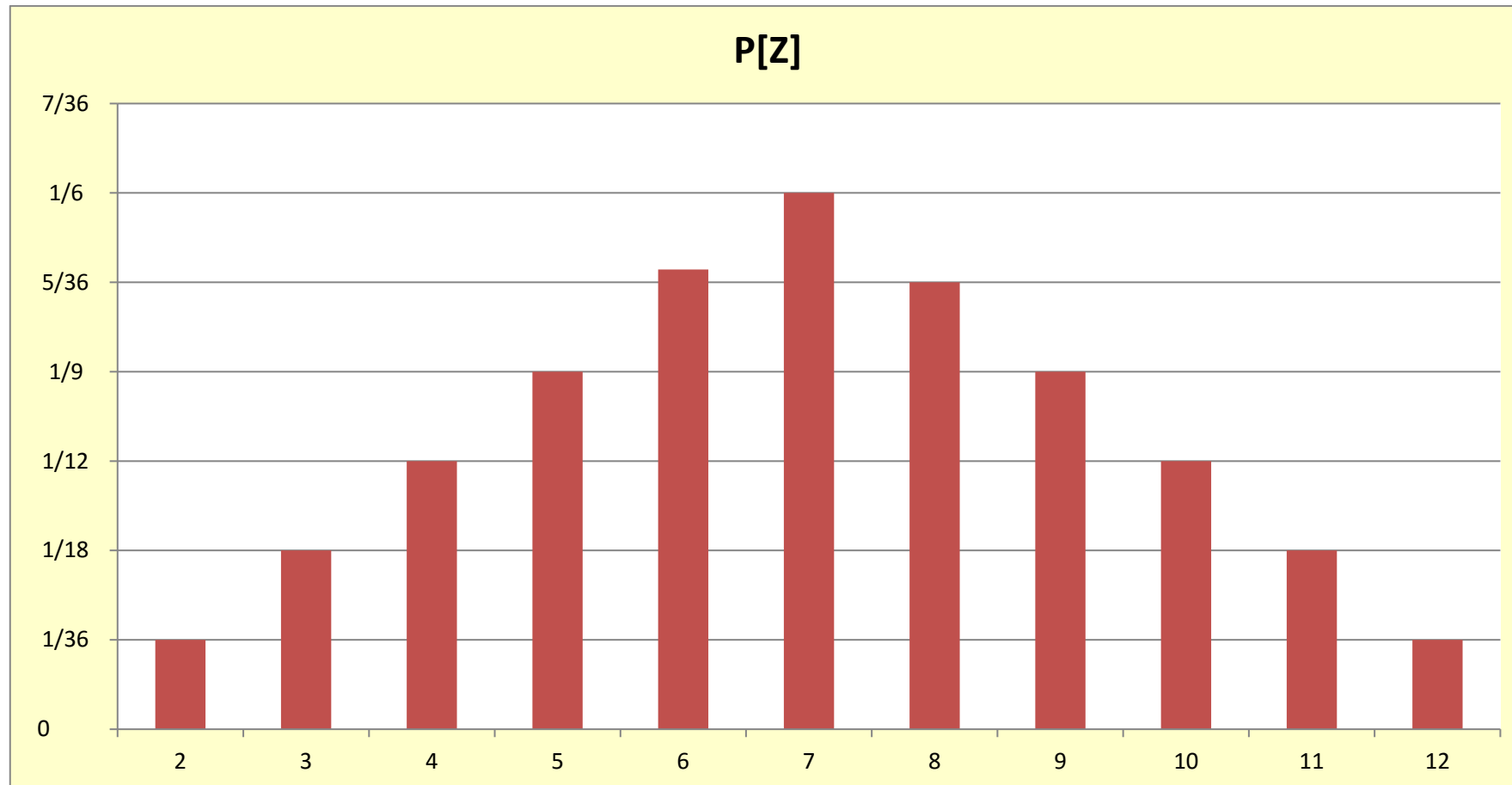
$$P[Z = 3] = 2/36$$

$$P[Z = 7] = 6/36$$

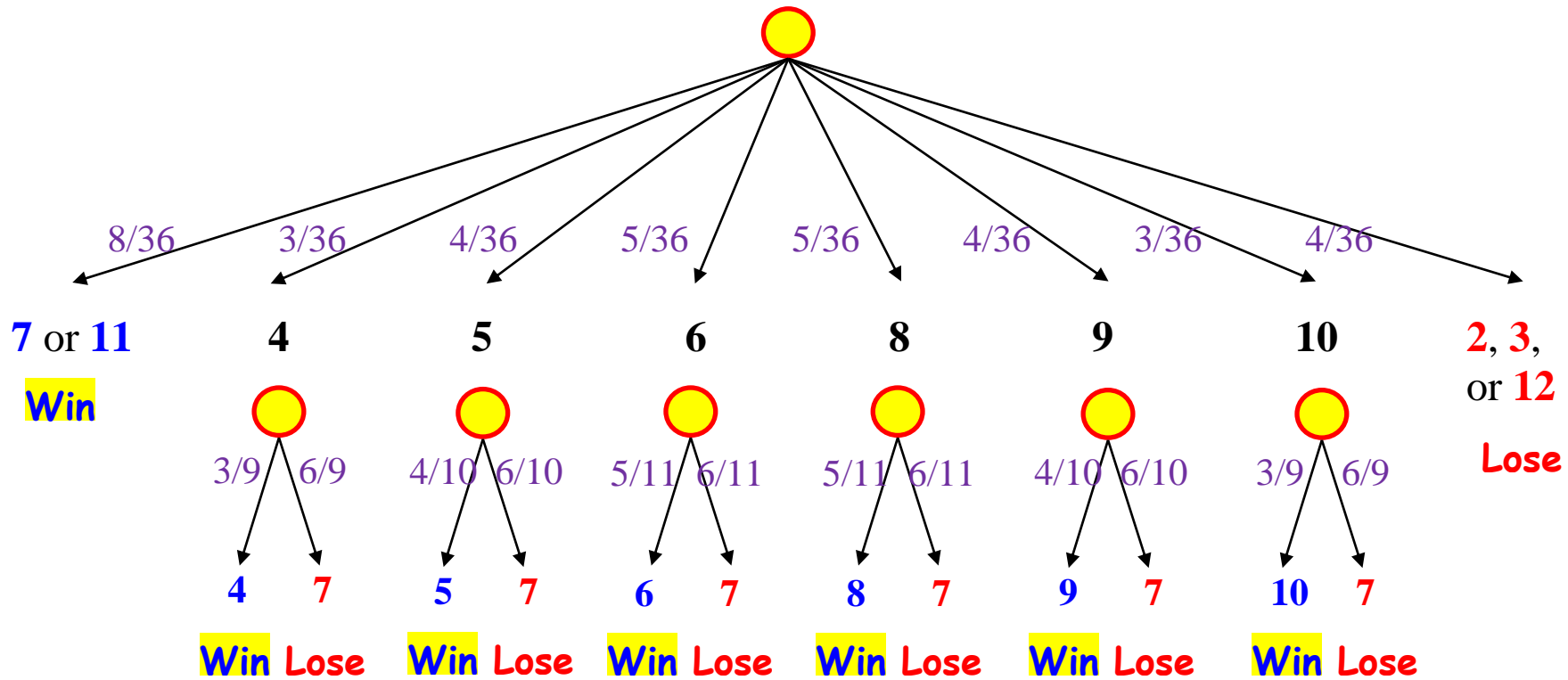
$$P[\text{Snake eyes}] = 1/36$$



- Probability Distribution of Z (Sum of the two numbers)



Z	2	3	4	5	6	7	8	9	10	11	12
P[Z]	1/36	2/36	3/36	4/36	5/36	6/36	5/36	4/36	3/36	2/36	1/36



■ Probability distribution

Z	2	3	4	5	6	7	8	9	10	11	12
P[Z]	1/36	2/36	3/36	4/36	5/36	6/36	5/36	4/36	3/36	2/36	1/36



- $P[\text{Win}]$

$$= 244/495 = 49.29\%$$

- Expected win on \$1 bet

$$= 1 * 244/495 + (-1) * 251/495 = - \$ 7/495$$

- House percentage (advantage)

$$= \text{Expected win} / \text{Amount of bet} * (-100) = 1.41\%$$

If you know the rules of the game, you can find $P[\text{Win}]!$

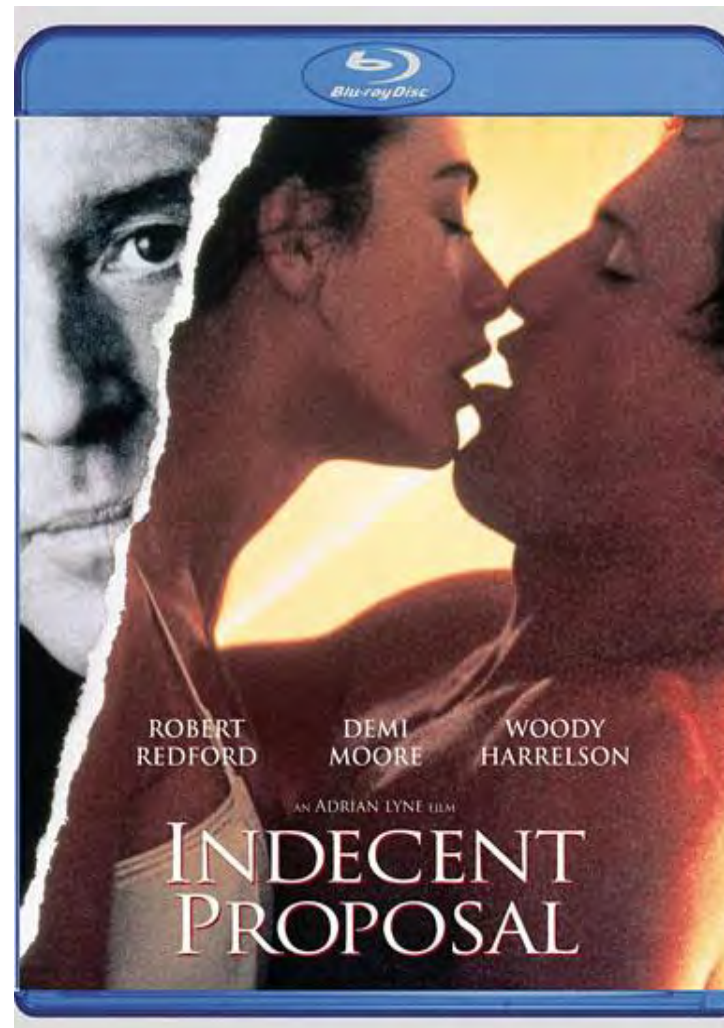


Movie Trivia



A husband. A wife. A millionaire. A proposal...
(Woody Harrelson, Demi Moore, and Robert Redford)

Indecent Proposal (1993)



A husband. A wife. A millionaire. A proposal...
(Woody Harrelson, Demi Moore, and Robert Redford)