

Dr. Chun's Numb3rs & Løgic

Simple Probability



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* Relative frequency

If there are n possible outcomes, all equally likely, and an event X occurs in k of these outcomes, we say that the probability of X is k/n and is denoted as $P[X]$.

Ex] A fair coin is tossed twice and observed to be either a head or a tail each time. Let X be the number of heads. Find the probability distribution of X .



- Sample space: $S = \{HH, HT, TH, TT\}$, where there are 4 possible outcomes
- Random variable: Let X be the number of heads.
- Probability distribution

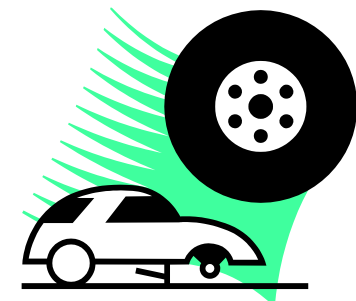
X	0	1	2
$P[X]$	$1/4$	$2/4$	$1/4$

Flat Tire

Ask Marilyn, Parade Magazine, (March 3, 1996), p. 14



At LSU, two students had received **A**'s in managerial statistics all semester. But on the night before the **final exam**, they were partying in New Orleans and didn't get back to LSU until it was over. Their excuse to the professor was that they had a **flat tire**, and they asked if they could take a **make-up test**.



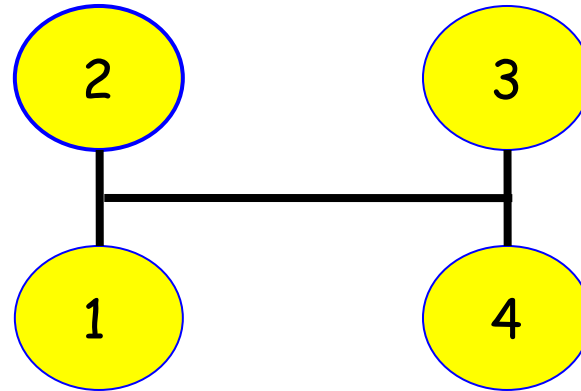
The professor agreed, wrote out a test and sent the two to **separate rooms** to take it. The **first question** (on one side of the paper) was worth 5 points, and they answered it easily. Then they flipped the paper over and found the **second question**, worth **95 points**: "Which tire was it?"

What was the **probability** that both students would say the same thing? My dad and I think it's **1 in 16**. Is that right?

- Heather Connell, New Freedom, Pa.



* Tires



* Sample space

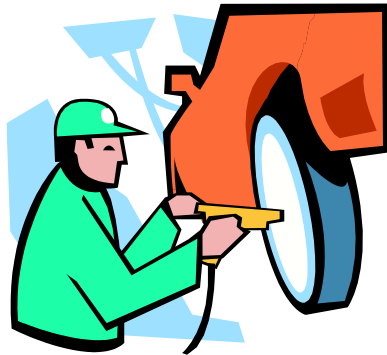
$$S = \left\{ \begin{array}{cccc} 11 & 12 & 13 & 14 \\ 21 & 22 & 23 & 24 \\ 31 & 32 & 33 & 34 \\ 41 & 42 & 43 & 44 \end{array} \right\}$$

* **Probability** of selecting the same numbers = $4/16 = 25\%$



* Heard from a local mechanic!

"The most likely tire to be punctured is the **right rear one**.



That is because road debris tends to accumulate at the **gutter side of the road**. The **front tire** is usually not damaged when it runs over something like a nail, because nails normally lie flat on the pavement.

However, the **front tire** may kick up the nail, so that before the nail has time to fall back, it is caught by the **right rear tire**."

* Flat tire!

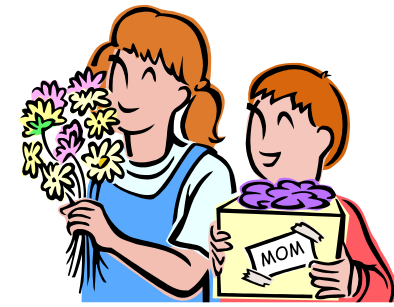
It will be the **right rear tire!**

Gift Exchange



From "Ask Marilyn," *Parade Magazine*, (September 13, 1992), p. 26

"After each holiday gift exchange, my **five** nieces and nephews write their names on slips of paper into a basket, from which they then draw the name of the person for whom they'll buy a gift the following year.



Last year, for the first time, each of the **five** drew his or her own name. What are the **chances** of such an occurrence taking place?

- Richard Coffey, Newington, Conn."

Adam

Brett

Cindy

David

Emily



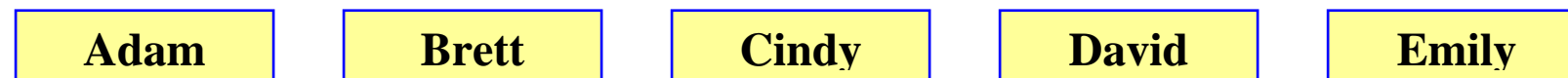
* Sample space?

1 Adam	2 Brett	3 Cindy	4 David	5 Emily
1	2	3	4	5
1	2	3	5	4
1	2	4	3	5
1	2	4	5	3
..
5	4	3	1	2
5	4	3	2	1

* Number of possible permutations?

$$5! = 120$$

* Probability of the **perfect match**?



$$\frac{1}{5} \cdot \frac{1}{4} \cdot \frac{1}{3} \cdot \frac{1}{2} \cdot \frac{1}{1} = 1/5! = \frac{1}{120}$$

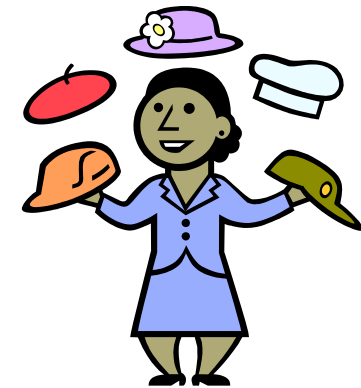


* Open question!

What is the **probability** that **none of the five kids** draw their own names?

* Hat-check problem

Suppose that **three guests** check their hats when they arrive at a restaurant, and that these hats are returned to them **in a random order** when they leave. Determine the probability that **no guest** will receive the proper hat.



Guest 1	1	1	2	2	3	3
Guest 2	2	3	1	3	1	2
Guest 3	3	2	3	1	2	1
Match?	3	1	1	0	0	1

▪ $P[\text{No Match}] = \frac{2}{6}$

Ask Marilyn, Parade Magazine (May 11, 2003), page 17



"Twenty kids throw their hats into a box. They then close their eyes, and each randomly withdraws a hat. What is the probability that 19 of the kids will withdraw their own hats?"

George Padgett, Greenville, S.C.



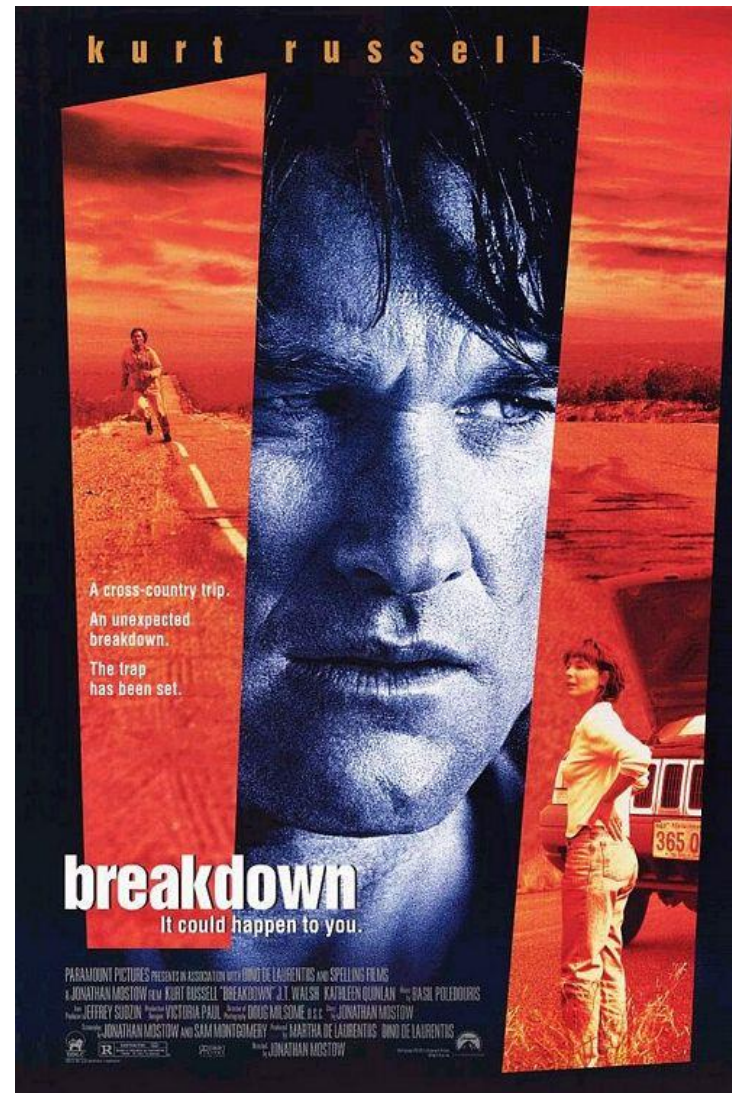
■ $P[X=19 \text{ matches} \mid n=20 \text{ hats}] = 0$

Movie Trivia



A man searches for his missing wife
after **his car** breaks down in the middle of the desert.

Breakdown (1997)



A man searches for his missing wife after his car breaks down in the middle of the desert.