

Dr. Chun's Numb3rs & Løgic

Simpson's Paradox



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Simpson's Paradox

Large corporations and companies are divided into several divisions, subdivisions, departments, and so on. Except for high-level managerial positions, employment decisions usually take place at the departmental or divisional level. Analyzing **aggregate employment data** in such companies can give rise to a curious phenomenon known as **Simpson's paradox**.

An instructive and surprising example of **Simpson's paradox** occurred at the **University of California at Berkeley** in the 1970s. Examination of applicant data for a 1973 quarter revealed that the **overall rate** of admission for **female** applicants to the graduate school was substantially less than the rate of admission for **male** applicants.



Which departments at **Berkeley** were responsible for this imbalance?



Applicants to UC Berkeley		Number applied	Number admitted	Percent admitted
Combined	Male	110	91	82.7%
	Female	110	19	17.3%

* Hypothesis

$$H_0: \pi_f \geq \pi_m$$

$$H_1: \pi_f < \pi_m$$

* Test statistic:

$$z^* = \frac{(\bar{p}_1 - \bar{p}_2)}{\sqrt{\bar{p}(1 - \bar{p})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} = 9.7$$

* One-sided **p-value**:

$$P[Z > 9.7] = 0.00$$





Applicants to UC Berkeley		Number applied	Number admitted	Percent admitted
Department of Mathematics	Male	100	90	90%
	Female	10	9	90%
Department of English	Male	10	1	10%
	Female	100	10	10%
Combined	Male	110	91	82.7%
	Female	110	19	17.3%

* **Department of Mathematics**

- Acceptance rate for **male** = $90/100 = 90\%$
- Acceptance rate for **female** = $9/10 = 90\%$

* **Department of English**

- Acceptance rate for **male** = $1/10 = 10\%$
- Acceptance rate for **female** = $10/100 = 10\%$

* **No discrimination at all !**

Ask Marilyn, Parade Magazine (4/28/1996), p. 6.



Applicants to a company		Number applied	Number admitted	Percent admitted
White-collar position	Male	200	30	15%
	Female	200	40	20%
Blue-collar position	Male	400	300	75%
	Female	100	85	85%
Combined	Male	600	330	55.00%
	Female	300	125	41.67%

- **White-collar position**
 - Discrimination against **male** applicants
- **Blue-collar position**
 - Discrimination against **male** applicants
- **Overall statistic?**
 - Discrimination against **female** applicants

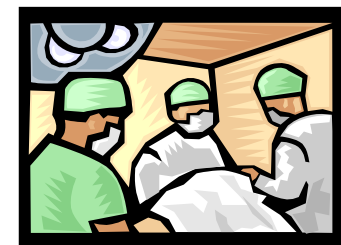


Ask Marilyn, Parade Magazine (4/28/1996), p. 6.



Patients		Sample size	Number cured	Percentage cured
Study 1	A	100	36	36%
	B	1,000	450	45%
Study 2	A	1,000	600	60%
	B	100	65	65%
Total	A	1,100	636	57.82%
	B	1,100	515	46.82%

- Study 1
 - Treatment B is more effective than A.
- Study 2
 - Treatment B is more effective than A.
- Overall statistic?
 - Treatment A is more effective than B.





Batting Average of Two Baseball Players

A real-life example involves the **batting average** of two baseball players, **Derek Jeter** and **David Justice**, during the baseball years **1995** and **1996**:

	Player	Number of at-bats	Number of hits	Batting average
1995	Derek Jeter	48	12	.250
	David Justice	411	104	.253
1996	Derek Jeter	582	183	.314
	David Justice	140	45	.321
Total	Derek Jeter	630	195	.310
	David Justice	551	149	.270

In both 1995 and 1996, **Justice** had a higher **batting average** (in bold type) than **Jeter** did.

However, when the two baseball seasons are combined, **Jeter** shows a higher **batting average** than **Justice**.



The moral of the story is...



- "You can prove **anything** with **statistics!**"
- "There are lies, damn lies, and **statistics!**"



The **aim** of this course is to enhance your ability to draw insight from data and to assess more precisely the reliability of your inferences.

Because statistics are frequently "**misused** to give an air of legitimacy to weak claims," the course also aims to make you better **consumers** of statistical analyses conducted by others.

Movie Trivia



Oakland A's general manager Billy Beane's successful attempt to assemble a **baseball team** on a lean budget by employing computer-generated analysis to acquire new players.

Moneyball (2011)



Oakland A's general manager Billy Beane's successful attempt to assemble a baseball team on a lean budget by employing computer-generated analysis to acquire new players.