

Dr. Chun's Numb3rs & Løgic

The Pirate Game



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The Pirate Game

There are five *rational* pirates, A, B, C, D and E. They find 100 gold coins. They must decide how to distribute them. The Pirates have a strict order of *seniority*: A is superior to B, who is superior to C, who is superior to D, who is superior to E.

The Pirate world's *rules of distribution* are as follows: The most senior pirate should propose a distribution of coins. The pirates should then vote on whether to accept this distribution; the proposer is able to vote, and has the *casting vote* in the event of a tie. If the proposed allocation is approved by vote, it happens. If not, the proposer is thrown overboard from the pirate ship and dies, and the next most senior pirate makes a new proposal to begin the system again.

Find the *optimal strategy* for A.





* Backward Iterations: Start from the last step!

- Step 4. (D, E)

D=100 E=0

- Step 3. (C, D, E)

- Step 2. (B, C, D, E)

- Step 1. (A, B, C, D, E)





* Backward Iterations: Start from the last step!

- Step 4. (D, E)

D=100 E=0

- Step 3. (C, D, E)

C=99 D=0 E=1

- Step 2. (B, C, D, E)

- Step 1. (A, B, C, D, E)





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- Step 4. (D, E)

$$D=100 \quad E=0$$

- Step 3. (C, D, E)

$$C=99 \quad D=0 \quad E=1$$

- Step 2. (B, C, D, E)

$$B=99 \quad C=0 \quad D=1 \quad E=0$$

- Step 1. (A, B, C, D, E)





* Backward Iterations: Start from the last step!

- Step 4. (D, E)

$$D=100 \quad E=0$$

- Step 3. (C, D, E)

$$C=99 \quad D=0 \quad E=1$$

- Step 2. (B, C, D, E)

$$B=99 \quad C=0 \quad D=1 \quad E=0$$

- Step 1. (A, B, C, D, E)

$$A=98 \quad B=0 \quad C=1, \quad D=0 \quad E=1$$



The **pirate game** is a simple mathematical game that illustrates how, if assumptions conforming to a *homo economicus* model of human behavior hold, outcomes may be **surprising**!

The Ultimatum Game



The so-called "**ultimatum game**" generally involves two players: One is given a certain amount of money, say **\$100**, by an **experimenter**, and the other is given a kind of **veto**.

The **first player** may offer any nonzero fraction of the \$100 to the **second player**, who can either **accept** or **reject** it. If he **accepts** it, he is given whatever amount the first player has offered, and the first player keeps the balance. If he **rejects** it, the **experimenter** takes the \$100 back.



Viewing this in **rational** game-theoretic terms, one would argue that it's in the interest of the second player to accept whatever is offered, since **any amount**, no matter how small, is better than **nothing**.

This is not what happens, however. When the offers deemed **too small**, the offers are often **rejected**. The resentful rejecters say that "**better to receive nothing than to be humiliated**". Notions of **fairness** and **equity**, as well as **anger** and **revenge**, seem to play a role.



Homo economicus, or **Economic man**, is the concept, in some economic theories, of man (that is, a human) as a rational, perfectly informed, and self-interested actor who desires wealth, avoids unnecessary labor, and has the ability to make judgments towards those ends.



- Do you think the **pirates** are **Homo economicus**?
- Are you?
- **Homo economicus** is a valid **assumption** or a **myth**?

"Irrational exuberance" during the Dot-com bubble of the 1990s...

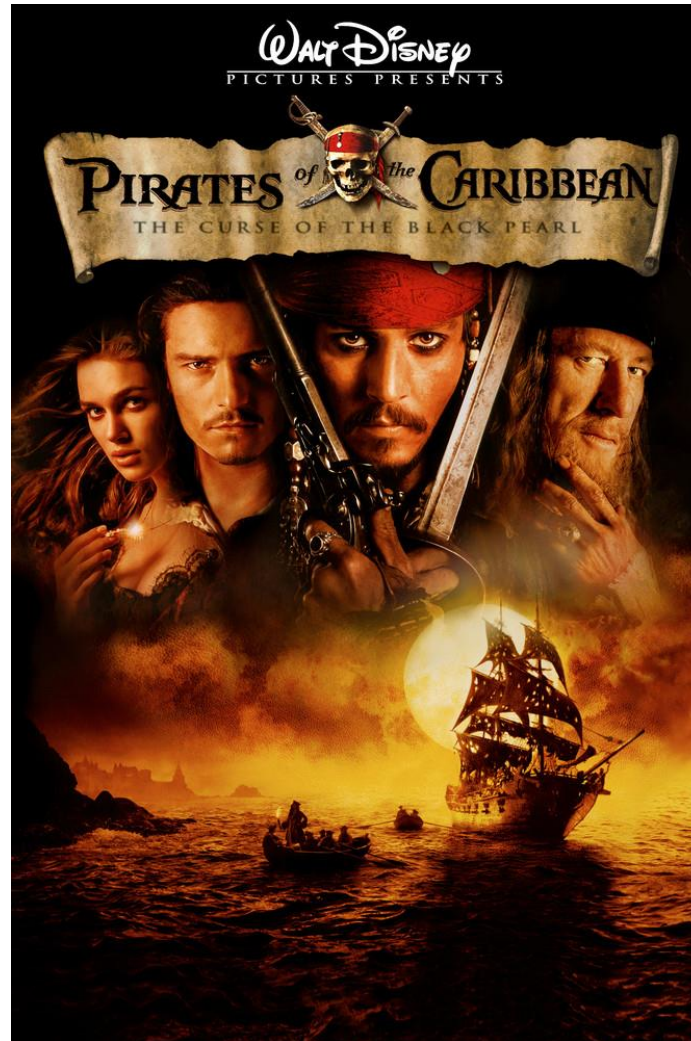
- **Alan Greenspan**, Chairman of **Federal Reserve** (1987~2006)

Movie Trivia



Blacksmith **Will Turner** teams up with eccentric pirate "**Captain**" **Jack Sparrow** to save his love, the governor's daughter, from Jack's former pirate allies, who are now undead.

Pirates of the Caribbean (2003)



Blacksmith **Will Turner** teams up with eccentric pirate "**Captain**" **Jack Sparrow** to save his love, the governor's daughter, from Jack's former pirate allies, who are now undead.